

CHAPTER IV

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PROGRAM LISTING

```
/*----- */
/* This is the main program. In this program the
   Eigenvalues & Eigenvectors of the matrix is computed. */
/*----- */

#include <stdio.h>
#include <math.h>
#include "mhb2.c"
#include "jb.c"
#include "given.c"
#define MAXROWS 5
#define MAXCOLS 5

extern void read_mat(int r1,int c1,double temp[5][5]);
extern void print_mat(int r1,int c1,double temp[5][5]);
extern void mat_mul(int r1,int c1,double x1[5][5],
                   double y1[5][5],double z1[5][5]);
extern void jb_mat(int r1,int c1,double a[5][5],
                  double p[5][5],double s[5][5],double ev[5][5],double
v[5][5],
                  double b[5][5],double max );
extern void gn_mat(int r1,int c1,double a[5][5],double s[5][5],
                  double p[5][5]);
```

```
main()

{
    int rows,cols;
    double a[MAXROWS][MAXCOLS];
    double s[MAXROWS][MAXCOLS];
    double p[MAXROWS][MAXCOLS];
    double ev[MAXROWS][MAXCOLS];
    double b[MAXROWS][MAXCOLS];
    double v[MAXROWS][MAXCOLS];
    double max;
    int Method;

    printf("Give the numbers of rows\n");
    scanf("%d",&rows);
    printf("Give the numbers of cols\n");
    scanf("%d",&cols);
    printf("Enter the elements of the matrix\n");
    read_mat (rows,cols,a);
    printf("\n1 Jacobi method\n");
    printf("\n2 power method\n");
    printf("\n3 Given's method\n");
    printf("\Choose the method\n");
    scanf("%d",&Method);
```

```
switch (Method) {  
  
    case 1:  
  
        jb_mat(rows, cols, a, s, p, ev, v, b, max );  
        break;  
  
    case 2:  
  
        power_mat(rows, cols, a);  
        break;  
  
    case 3:  
  
        gn_mat(rows, cols, a, s, p);  
        break;  
  
    default:  
        break;  
  
}
```

```
/* The end of the program. */
```

```
/* This file contains functions */

void read_mat(int r1,int c1,double temp[5][5])

/* This function is for reading the matrix */

{
    int i, j;
    for(i=0;i<r1;i++)
    {
        for (j=0;j<c1;j++)
        {
            fflush(stdin);
            scanf("%lf",&temp[i][j]);
        }
    }
    return;
}
```

```
void print_mat(int r1,int c1,double temp[5][5])
/* This function is to print the matrix */
{
    int i,j, *fp;

    for(i=0;i<r1;i++)
    {
        for (j=0;j<c1;j++)
        {
            printf("%10.5lf",temp[i][j]);

        }
        printf("\n");
    }
    return;
} .
```

```
double mat_max(int r1,int c1,double temp[5][5])
/* For finding the maximum element of a matrix */
{
    int i,j;
    double tmp1,tmp,max;
    tmp = temp[0][0];
    max = fabs(tmp);
    for(i=0;i<r1;i++)
    {
        for(j=0;j<c1;j++)
        {
            tmp1 = temp[i][j];
            if(fabs( tmp1) > max)
                max = fabs(tmp1);
        }
    }
    return(max);
}
```

```
double vect_max(int r1,double temp[5])
/* For finding the maximum element of a vector */
{
    int i;
    double tmp1,tmp,max;
    tmp = temp[0];
    max = fabs(tmp);
    for(i=0;i<r1;i++)
    {
        tmp1 = temp[i];
        if(fabs( tmp1) > max)
            max = fabs(tmp1);
    }
    return(max);
}
```



```
void power_mat(int r1,int c1,double temp[5][5])
/* The function power_mat
   Purpose
   This function obtains the largest eigenvalue
   and eigenvector of a matrix by
   Power method Description of parameters
   r1 The number of rows
   c1 The number of columns
   temp The given matrix */
{
  int i,j;
  int k;
  double v[5],u[5];
  double t,mx,e;
  int *fp;
  e = 0.0001;
  mx = 0.00;
  for(i=0;i<r1;i++) ,
  {
    v[i] = 1;
  }
  do {
    for (k=0; k<r1;k++)
    {
      u[k] = 0;
```

```
        for(j=0;j<c1;j++)
            u[k] = u[k] + temp[k][j]*v[j];
    }

    t = mx;

    mx = vect_max(r1,u);

    for(i = 0; i<r1;i++)
        v[i] = u[i]/mx;
} while(fabs(t - mx )>e);

fp = fopen("out.dat","a");

printf("\nThe largest eigenvalue\n");

printf("%lf",mx);

printf("\nThe eigenvector\n");

for(i=0;i<r1;i++)
{
    printf("%17.10lf",v[i]);
}

return;

}
```

```
void mat_tran(int r1,int c1,int temp[5][5])  
  
{  
  int i,j;  
  for(i=0;i<r1;i++)  
  {  
    for (j=0;j<c1;j++)  
    {  
      tran[i][j] = temp[j][i];  
    }  
    return;  
  }  
}
```

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A

```
void mat_mul(int r1,int c1,double x1[5][5],double
y1[5][5],double z1[5][5])
/* Matrix multiplication */
{
int i,j,k;
for(i=0;i<r1;i++)
{
for (j=0;j<c1;j++)
{
z1[i][j] = 0;
for(k = 0; k < r1; k++)
{
z1[i][j] = z1[i][j] + x1[i][k]*y1[k][j];
}
}
}
return;
}
double fab(double x)
{
double y;
if (x<0)
y=-x;
else y=x;
return(y);
}
```



```
/* Function jb_mat
```

```
  Purpose
```

```
  This function obtains Eigenvalues & Eigenvectors of a real
  symmetric matrix by JACOBI method
```

```
  Description of parameters
```

```
  r1 : The number of rows
```

```
  c1 : The number of columns
```

```
  a  : The given real symmetric matrix
```

```
  s  : The transformation matrix
```

```
  p  : The reduced diagonal matrix, whose diagonal elements are
       the eigenvalues of the matrix A and
```

```
  ev : The n x n matrix which is used for the storage of the
       eigenvectors of the given matrix
```

```
  v  : The eigenvector
```

```
  b  : The given matrix is stored in this matrix */
```

```
void jb_mat(int r1,int c1,double a[5][5],double s[5][5],double
p[5][5],
```

```
    double ev[5][5],double v[5][5],double b[5][5],double max )
```

```
{
```

```
  double y,z;
```

```
  int i,j,k,l,q,r,rows,cols;
```

```
  rows=r1;
```

```
  cols=c1;
```

```
  for (i=0;i<r1;i++) {
```

```
for(j=0;j<c1;j++) {  
    b[i][j] = a[i][j];  
}  
}  
for (i=0;i<r1;i++) {  
    for (j=0;j<c1;j++) {  
        if (i==j)  
            ev[i][j] = 1;  
        else  
            ev[i][j] = 0;  
    }  
}  
do  
{  
    max = fabs(a[0][1]);  
    q = 0;  
    r = 1;  
    for(k=0;k<r1;k++) {  
        for(l=k+1;l<c1;l++) {  
            if(fabs(a[k][l]) > (float)max)  
            {  
                max =fabs( a[k][l]);  
                r = l;  
            }  
        }  
    }  
}
```

```
        q = k;
    }
}
}
for(k=0;k<r1;k++)
{
for(l=0;l<c1;l++) {
    if(k == l)
        s[k][l] = 1;
    else
        s[k][l] = 0;
}
}
if(a[q][q] == a[r][r] )
{
    if (a[q][r] < 0 )
        z = -1;
    else
        z = 1;
}
else
{
    y = 2*a[q][r]/(a[q][q]-a[r][r]);
    z = (-1+sqrt(1+y*y))/y;
```

```
}  
s[q][q] = 1/sqrt(1+z*z);  
  
s[r][r] = s[q][q];  
s[q][r] = -z*s[q][q];  
s[r][q] = -1*s[q][r];  
for(k=0;k<r1;k++)  
{  
    for(l=0;l<c1;l++)  
    {  
        p[k][l] = 0;  
        for(q=0;q<r1;q++)  
        {  
            for(r=0;r<c1;r++)  
            {  
                p[k][l] = p[k][l] + s[q][k]*s[r][l]*a[q][r];  
            }  
        }  
    }  
}  
for(q=0;q<r1;q++)  
{  
    for(r=0;r<c1;r++)  
    {  
        a[q][r] = p[q][r];  
    }  
}
```



```
    }  
  }  
  mat_mul(rows, cols, ev, s, v);  
  for (i=0; i<r1; i++) {  
    for(j=0; j<c1; j++) {  
      ev[i][j] = v[i][j];  
    }  
  }  
}  
while (max > 0.0001);  
printf("The given matrix\n");  
print_mat( rows, cols, b);  
printf("\n\nThe eigenvalues\n\n");  
for(i=0; i<rows; i++)  
{  
  printf("    %17.10lf\n", p[i][i]);  
}  
printf("\n\nThe eigenvector\n\n");  
print_mat(rows, cols, v);  
}
```

```

void gn_mat ( int r1,int c1,double a[5][5],double s[5][5],
             double p[5][5])
/* Tridiagonal matrix by Given's method. */
/* The function gn-mat

Purpose

The matrix reduces to tridiagonal form

Description of parameters

r1 : number of rows.

c1 : number of columns.

a  : The given matrix.

s  : The orthogonal matrix.

p  : The tridiagonal matrix.          */
{
double z;
int rows,cols,i,j,k,l,q,r;
rows = r1;
cols = c1;
q = 0;
r = 2;
for(i=0;i<rows;i++)

{
for(j=i+2;j<cols;j++)
{
q = i+1;
r = j;

```

```
/* The S matrix */
for(k=0;k<rows;k++)
{
    for(l=0;l<cols;l++)
    {
        if(k == l)
            s[k][l] = 1;
        else
            s[k][l] = 0;
    }
}

z = a[i][j]/a[i][i+1];
s[q][q] = 1/sqrt(1+z*z);
s[r][r] = s[q][q];
s[q][r] = -z*s[q][q];
s[r][q] = -1*s[q][r];

for(k=0;k<rows;k++)
{
    for(l=0;l<cols;l++)
    {
        p[k][l] = 0;
        for(q=0;q<rows;q++)
        {
            for(r=0;r<cols;r++)
            {
```



```
        p[k][l] = p[k][l] + s[q][k]*s[r][l]*a[q][r];
    }
}
}
}
for(k=0;k<rows;k++)
{
    for(l=0;l<cols;l++)
    {
        a[k][l] = p[k][l];
    }
}
}
}

printf("\n");
printf(" The tridiagonal matrix\n");
    print_mat(rows,cols,p);
}
```

(4.2) OUTPUT OF THE PROGRAM

Give the numbers of rows : 4

Give the numbers of cols: 4

Enter the elements of the matrix

*** MENU ***

1 Jacobi method

2 power method

3 Given's method

Choose the method

2

The largest eigenvalue

98.521699

The eigenvector

-0.6039723419 ,

1.0000000000 ,

-0.2511351318,

0.1489534465

Give the numbers of rows : 4

Give the numbers of cols: 4

Enter the elements of the matrix

** MENU **

1 Jacobi method

2 power method

3 Given's method

Choose the method

1

The given matrix

7.00000	3.00000	2.00000	1.00000
3.00000	9.00000	-2.00000	4.00000
2.00000	-2.00000	-4.00000	2.00000
1.00000	4.00000	2.00000	3.00000

The eigenvalues

5.7830521572

12.7198575387

-5.6002432141

2.0973335182

The eigenvector

0.85021	0.48325	-0.17742	-0.11013
-0.44325	0.79027	0.24328	-0.34614
0.23051	0.00833	0.90424	0.35937
-0.16593	0.37665	-0.30280	0.85960

Give the numbers of rows : 5

Give the numbers of cols : 5

Enter the elements of the matrix

** MENU **

1 Jacobi method

2 power method

3 Given's method

Choose the method

3

The given matrix

10.0000	1.00000	2.00000	3.00000	4.00000
1.00000	9.00000	-1.00000	2.00000	-3.00000
2.00000	-1.00000	7.00000	3.00000	-5.00000
3.00000	2.00000	3.00000	12.0000	1.00000
4.00000	-3.00000	-5.00000	-1.00000	15.0000

The Tridiagonal Matrix

10.0000	5.47723	0.00000	0.00000	0.00000
5.47723	10.8333	4.56321	0.00008	0.00000
0.00000	4.56321	8.56682	-5.62814	0.00000
0.00000	0.00000	-5.62814	14.13994	0.51925
0.00000	0.00000	0.00008	0.51925	9.36990

(4.3) CONCLUSION

While computing the eigenvalues and eigenvectors of a Hermitian or real symmetric matrix, the Jacobi method can be used. For a more general eigenvalue problem of the type $Ax = \lambda Bx$, where A is real symmetric and positive definite, again the Jacobi method may be used.

If the given square matrix A is nonsymmetric and real, and a good symmetrizer can be computed, then we compute a symmetrizer of A and next solve this symmetric eigenvalue problem, using the Jacobi method.

When we want to compute only the largest magnitude eigenvalue and its corresponding eigenvector, then the Power method is used.

It should be noted that no stable method is yet available for obtaining the eigenvalues of a nonsymmetric matrix.

In Jacobi method at each stage in the reduction of a real symmetric matrix to diagonal form, one must work with complete matrix. Here the elements reduced to zero in one rotation may become nonzero in other rotation, so the process may be infinite in case of larger matrix.

In Given's method an element reduced to zero in one rotation never becomes nonzero in latter rotations. After reducing the matrix to its tridiagonal form one can obtain its eigenvalues using Sturm sequence property or any other method for obtaining roots of a polynomial.

*** **

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